

# The GPS-SLR bias: dynamics, attitude and current experiments

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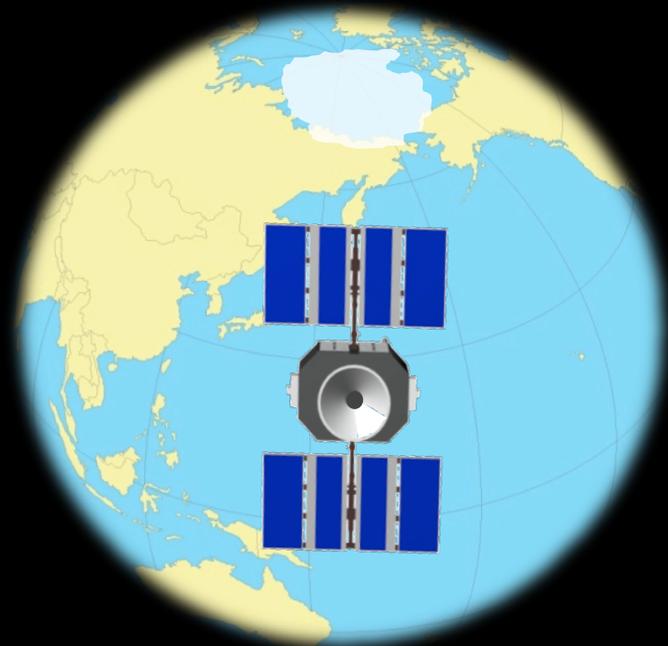
Tim Springer, Claudia Flohrer

ESOC

Ant Sibthorpe, Bruce Haines,

Yoaz Bar-Sever

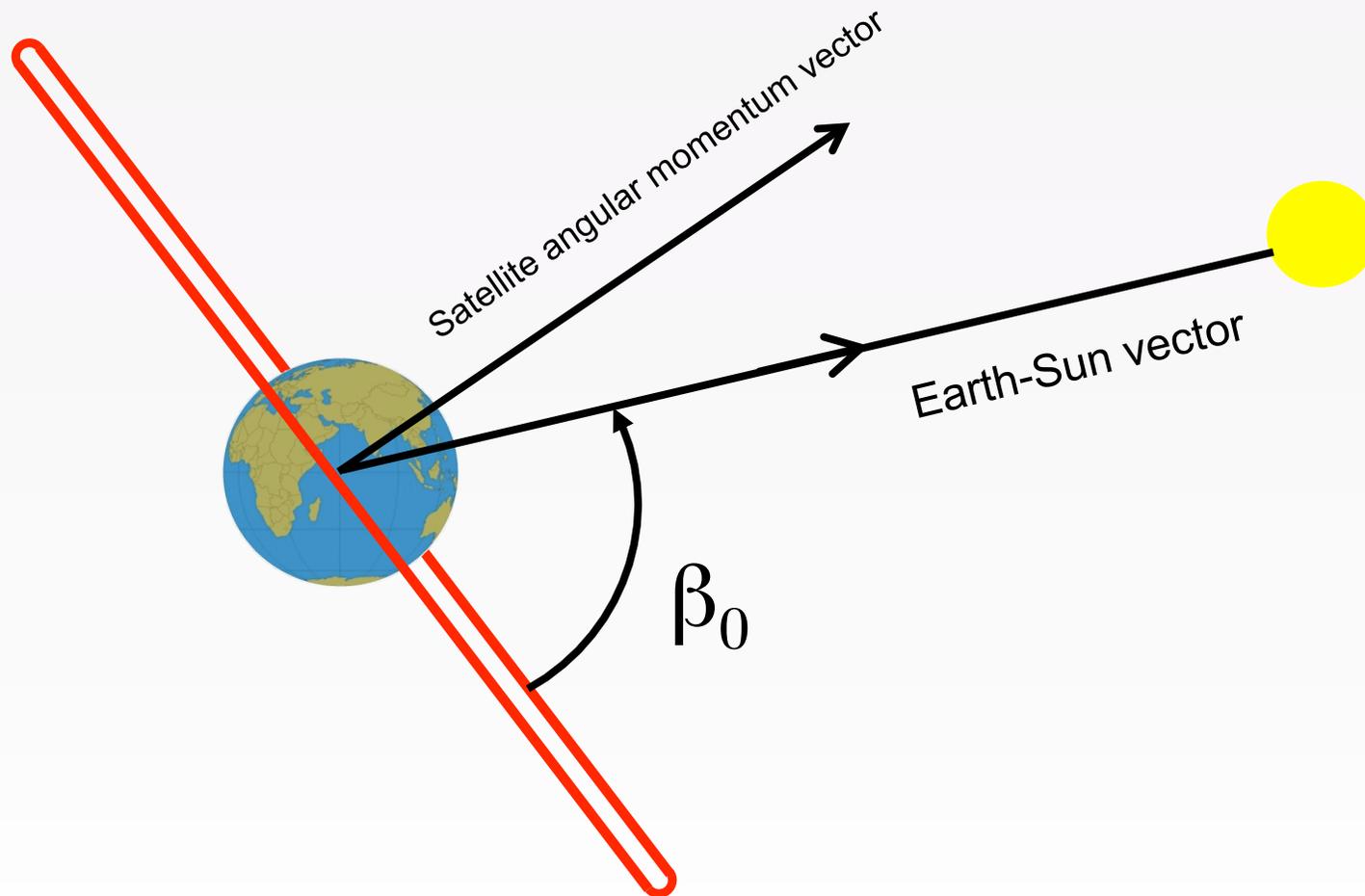
JPL



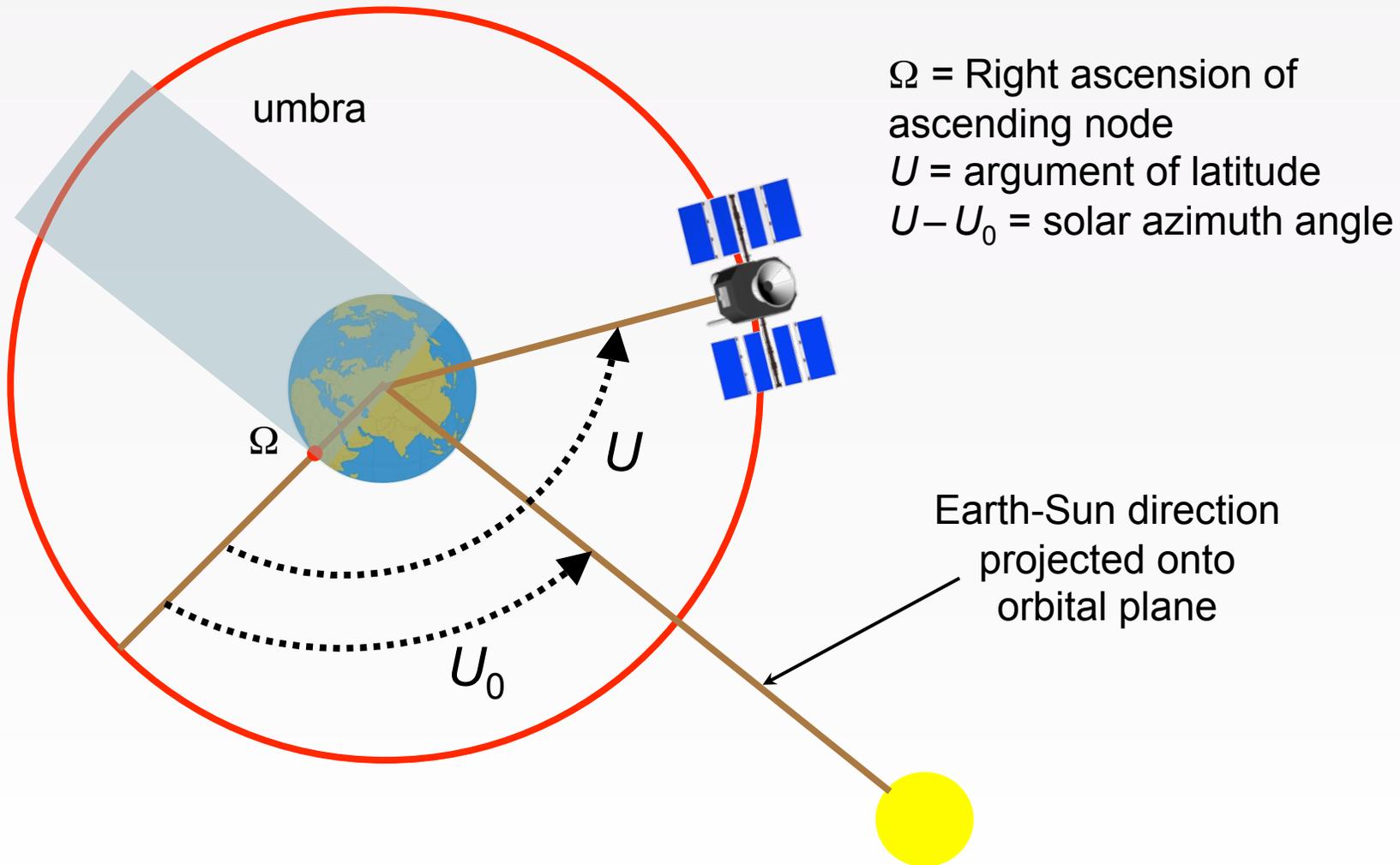
## Issues addressed in presentation:

- Characterisation of the GPS-SLR bias
- Force modelling approaches that significantly reduce the bias
- Physical explanation for the improvements
- Issues concerning Block IIA attitude
- Implementation issues/choices
- On going experiments

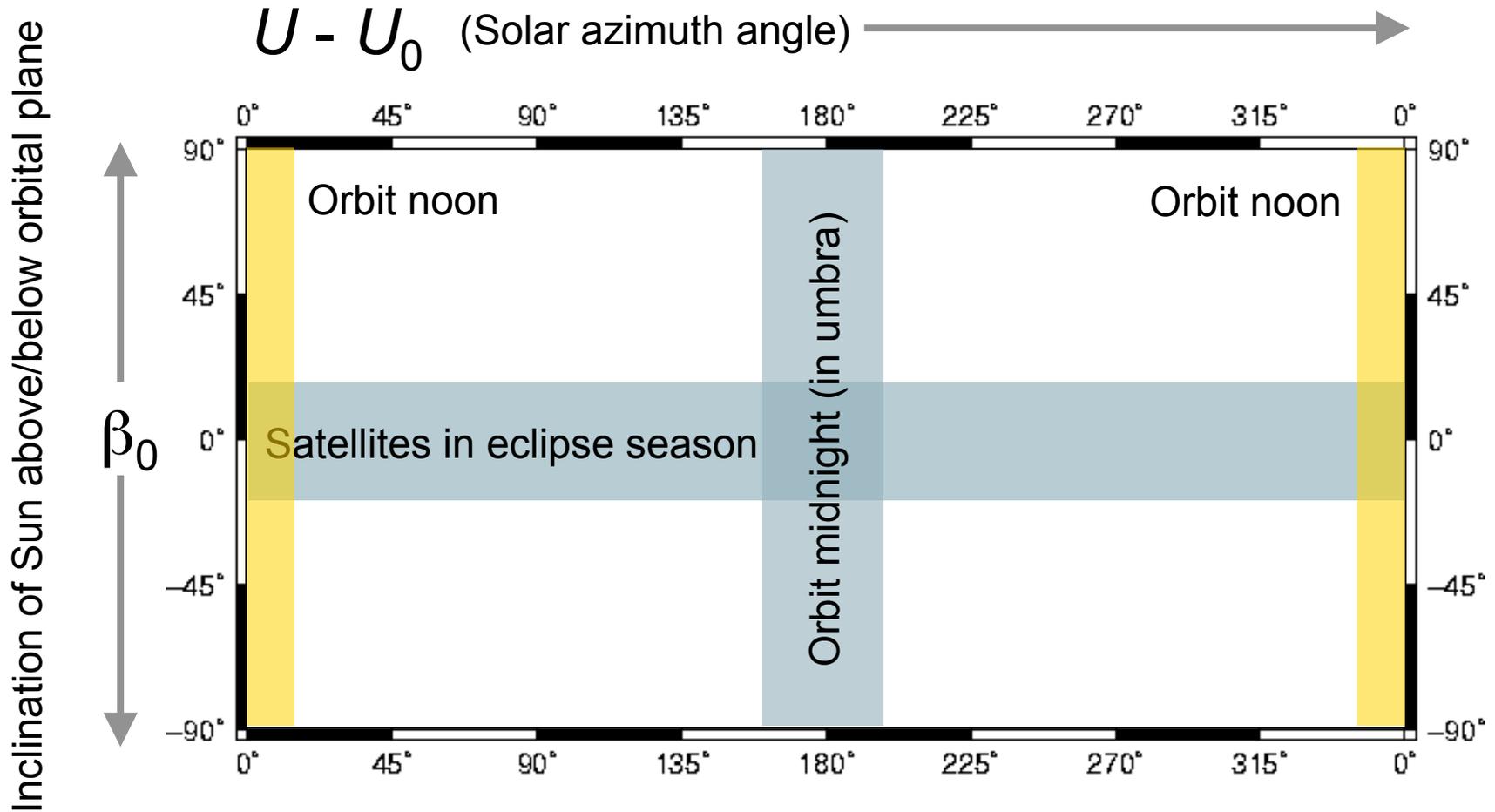
## Defining $\beta_0$

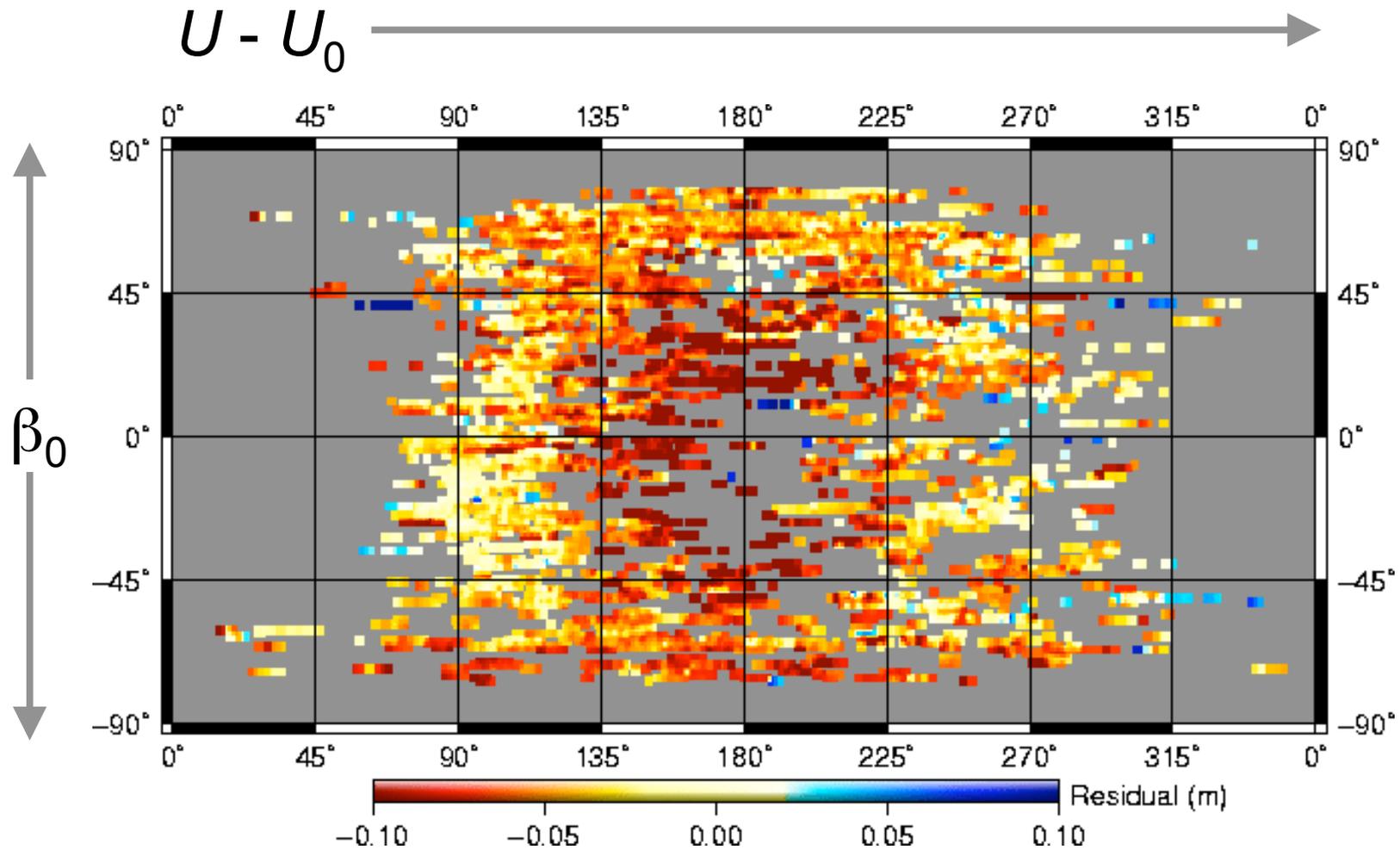


# Defining $U-U_0$ (solar azimuth angle)



# Plot used to characterise SLR – GPS residuals



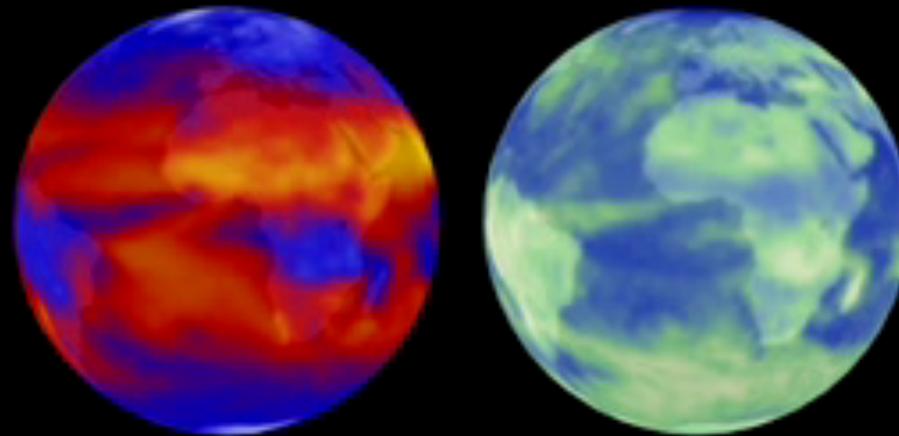


SLR – GPS two way range residuals  
(divide by two for range residuals)

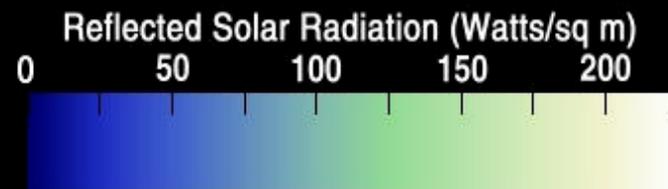
## Progress in attacking the GPS - SLR bias

- Several groups have experimented with planetary radiation pressure models (UCL/JPL, ESOC, CNES)
- All report significant reduction in bias
- What characterises these forces?
- Why do they impact upon the bias?
- What should we do next?

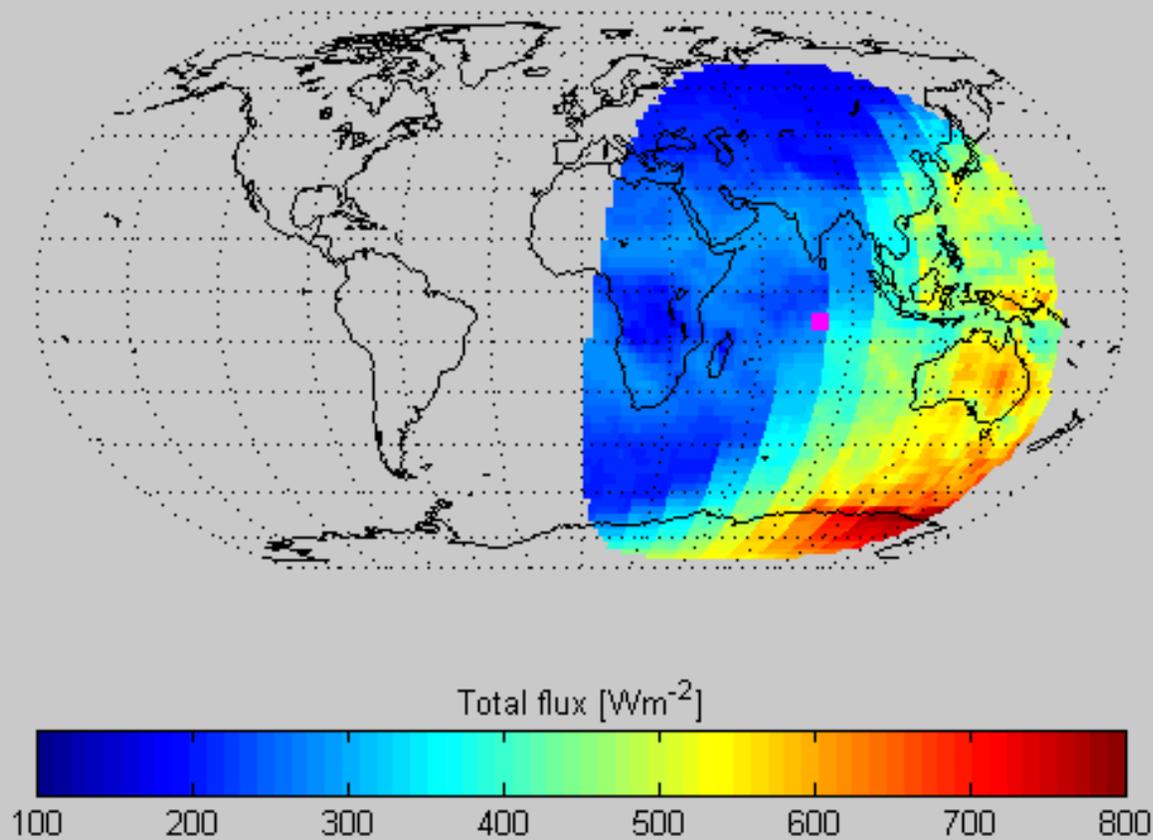
# Earth radiation flux patterns



Mar 2000



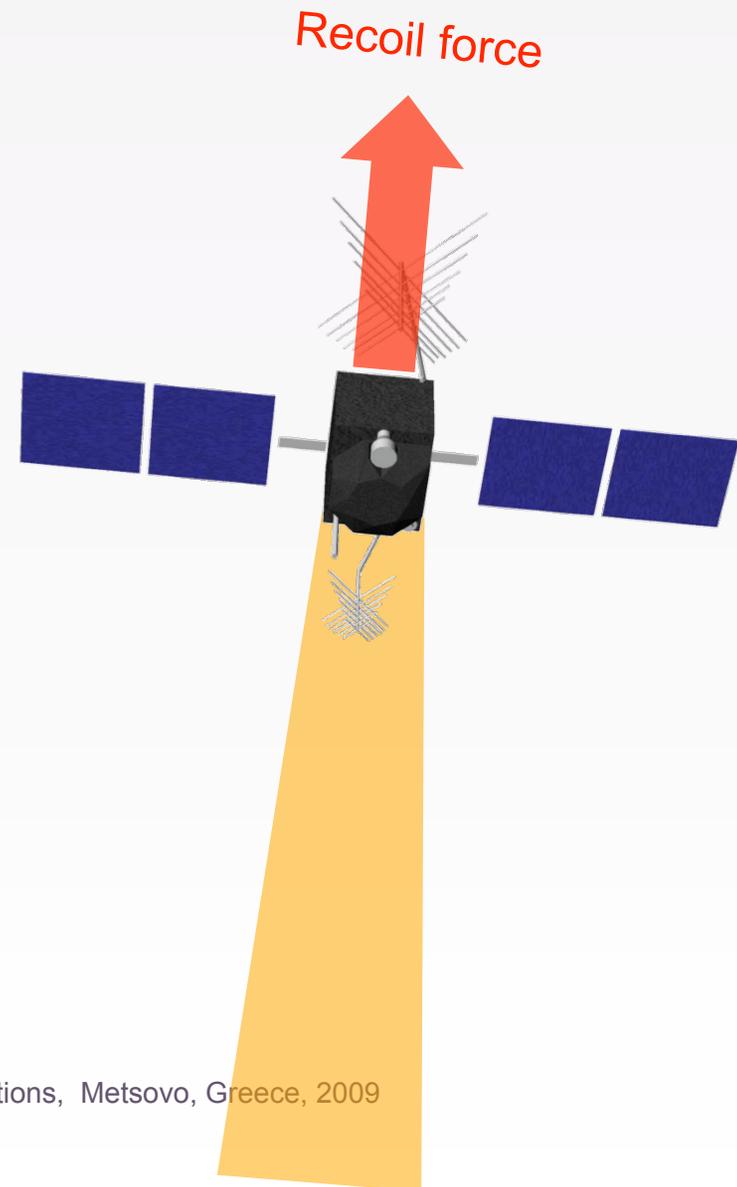
(01/96) 15 December 2003 00:14:47 -- SVN 13



# Radiation flux visible to SVN13, Dec 15<sup>th</sup> 2003

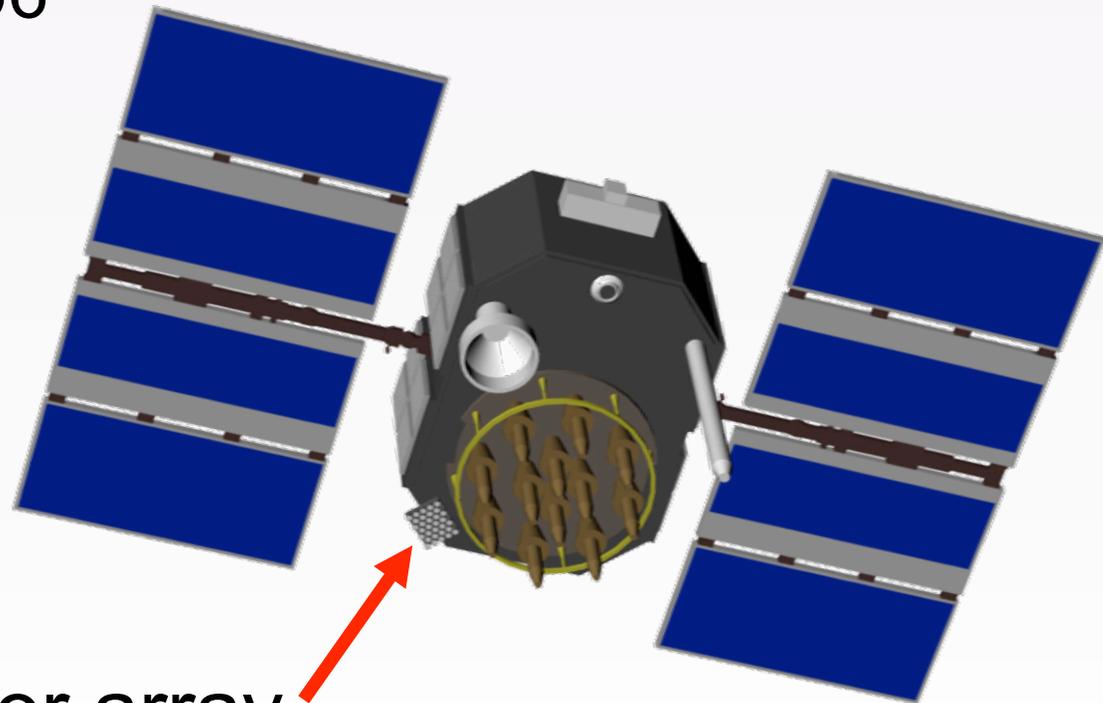
## Antenna Thrust (AT)

- Recoil force on satellite due to transmitted L1/L2 carriers
- Systematic and observable effect
- Requires knowledge of power transmission of satellites



## GPS satellites carrying retro-reflectors

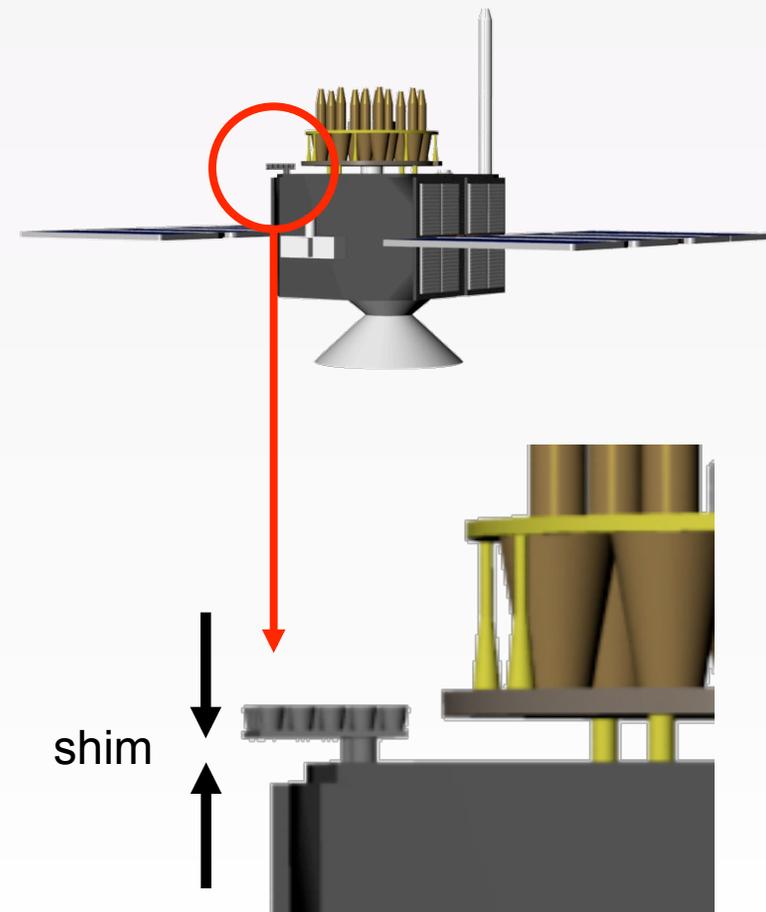
- 2 Block IIA spacecraft
- PRN05, PRN06



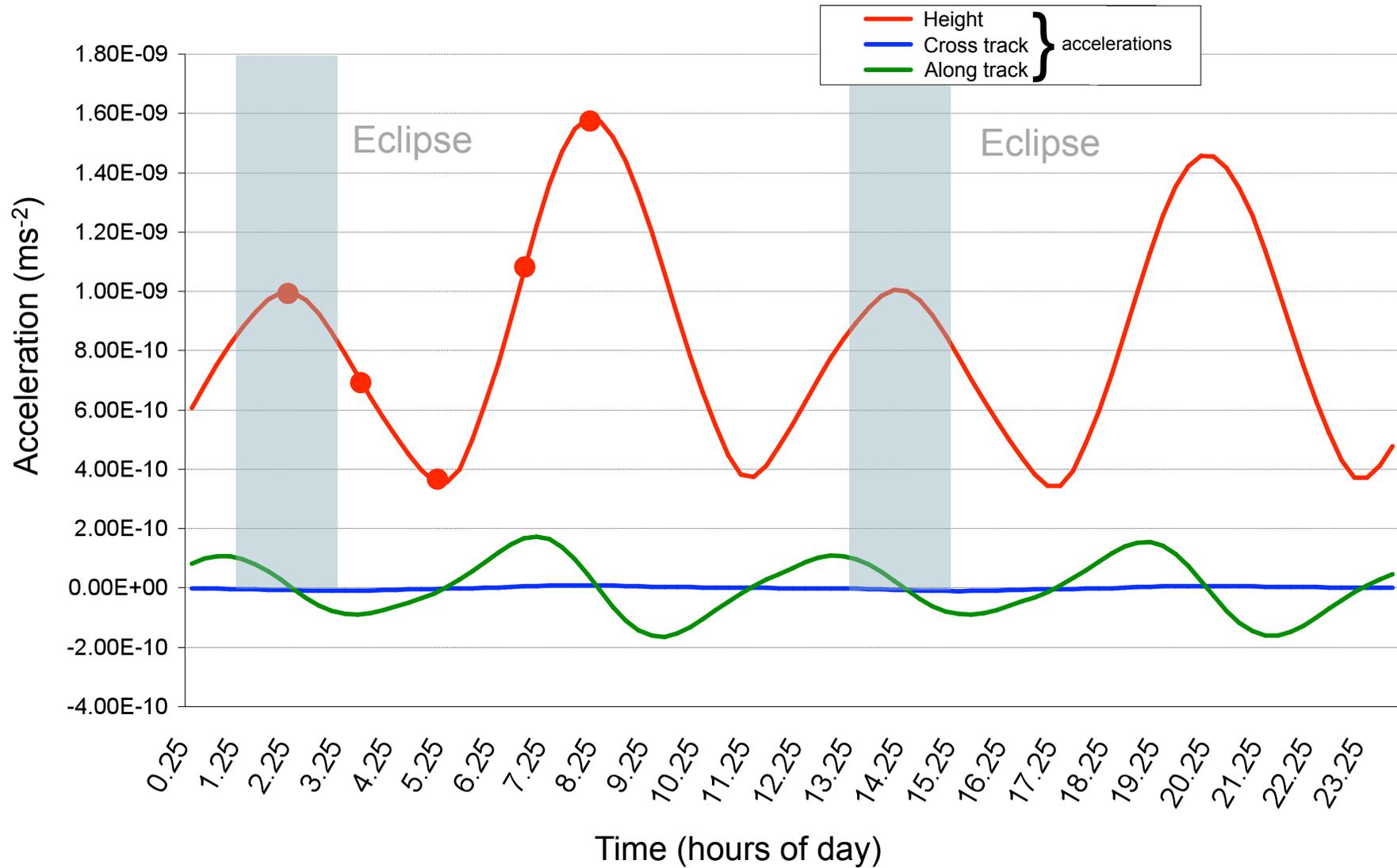
Retro-reflector array

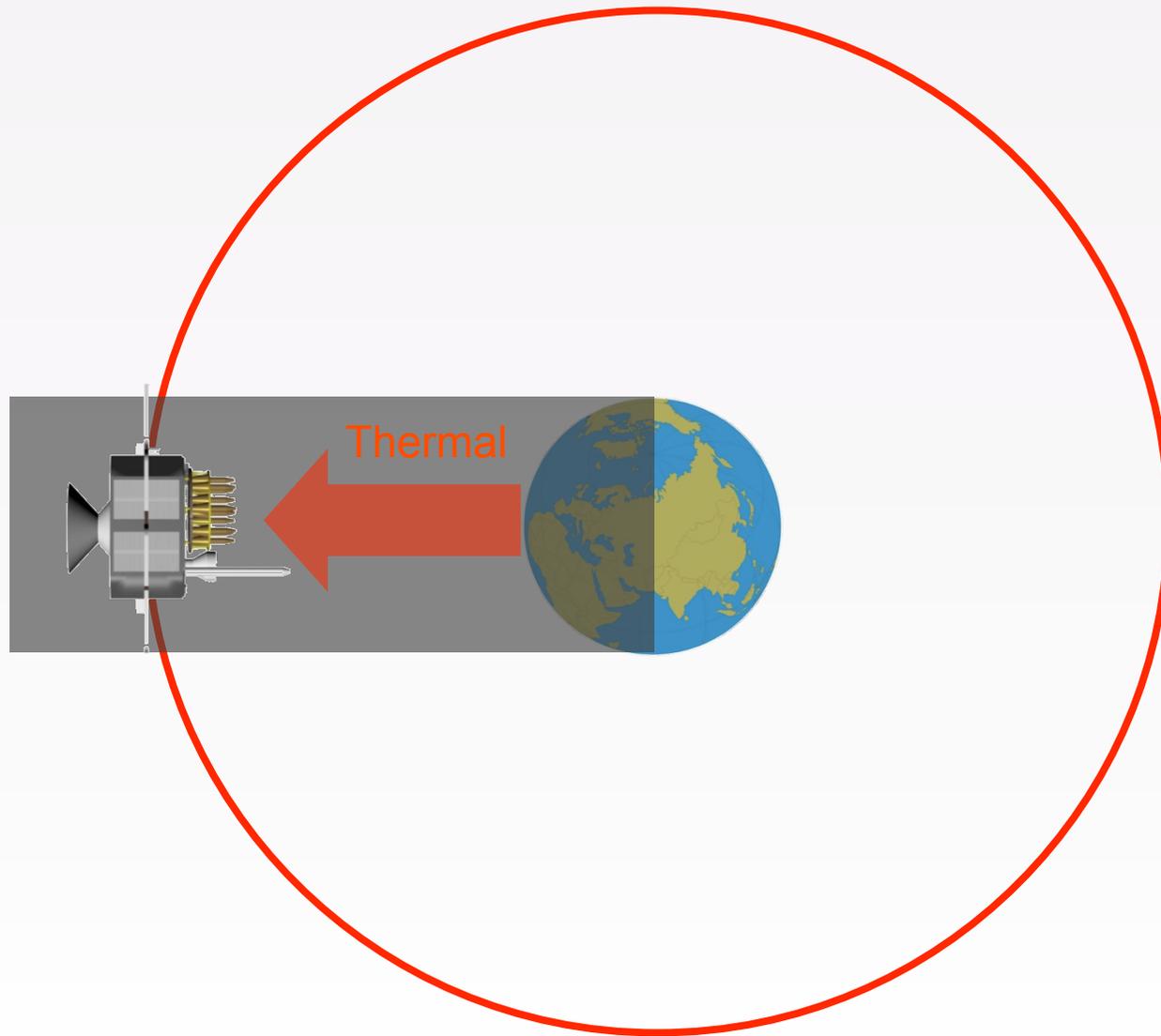
## Laser Retro-reflector Array (LRA) offset

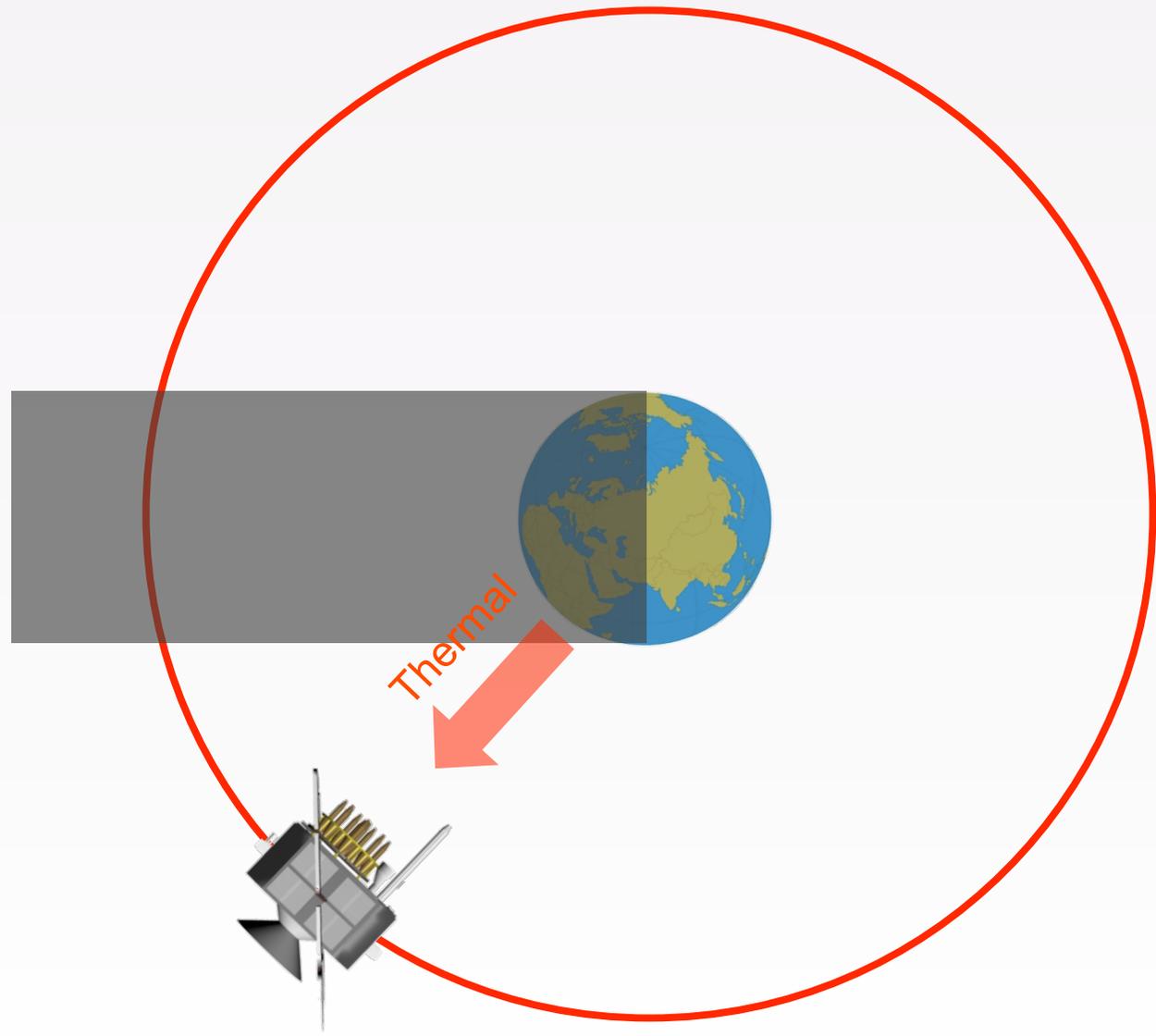
- LRA position in s/c body frame required for analysis of laser ranging
- New data suggests LRA offset further from centre of mass than previously understood
- Shim corrections: +11 mm (PRN05), +13 mm (PRN06)

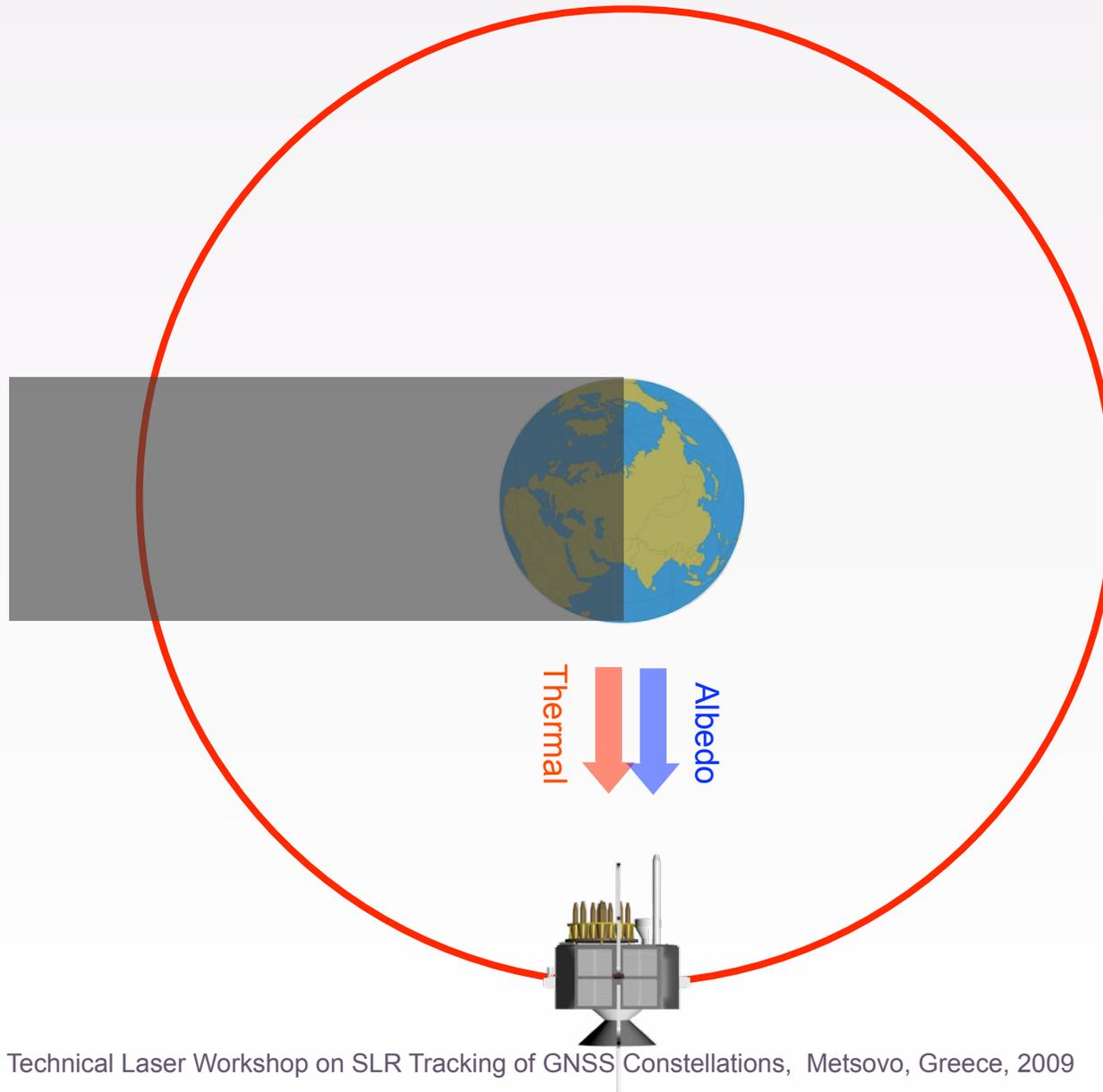


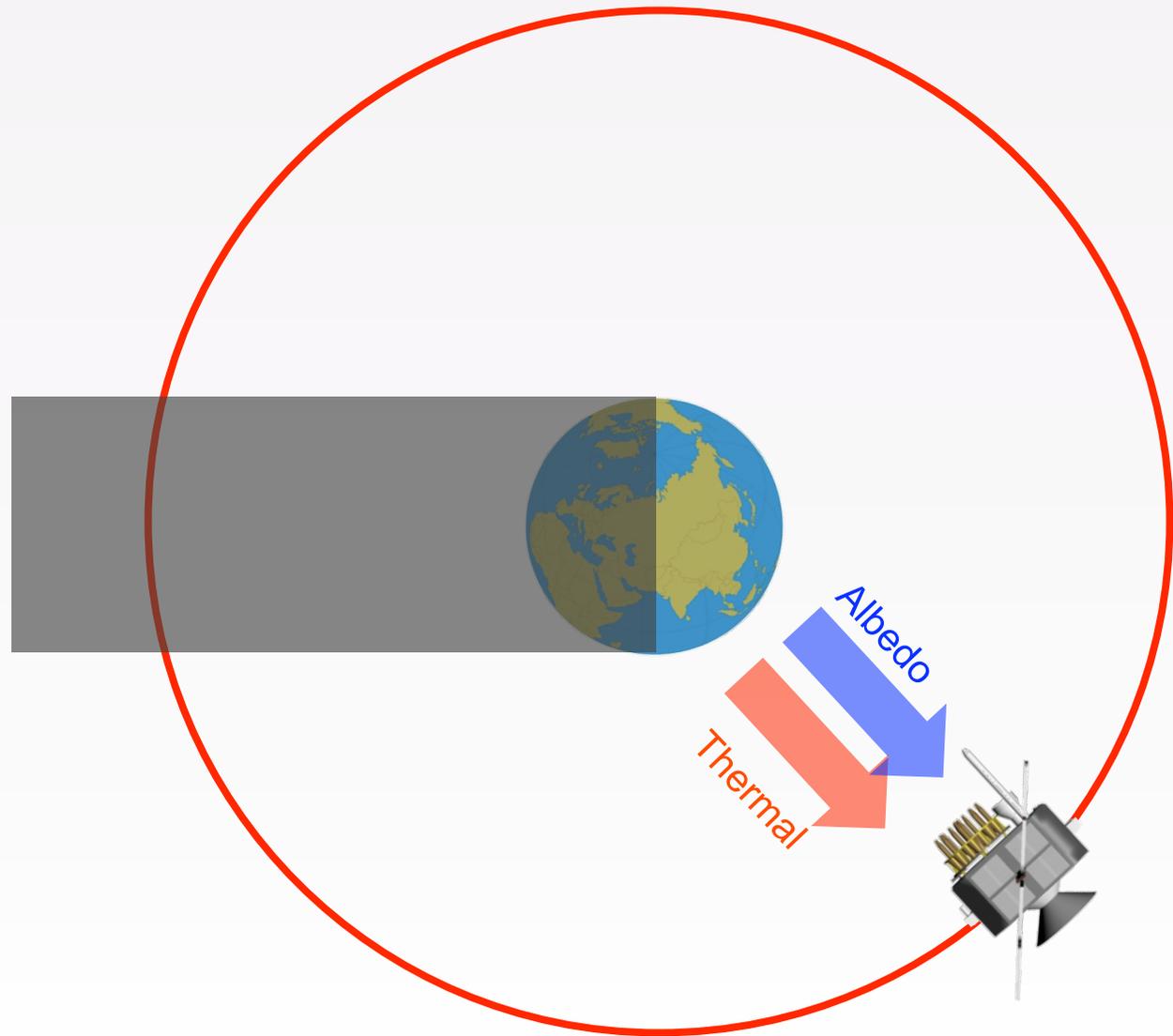
Modelled Earth Radiation pressure (SVN35, UCL ADM model)

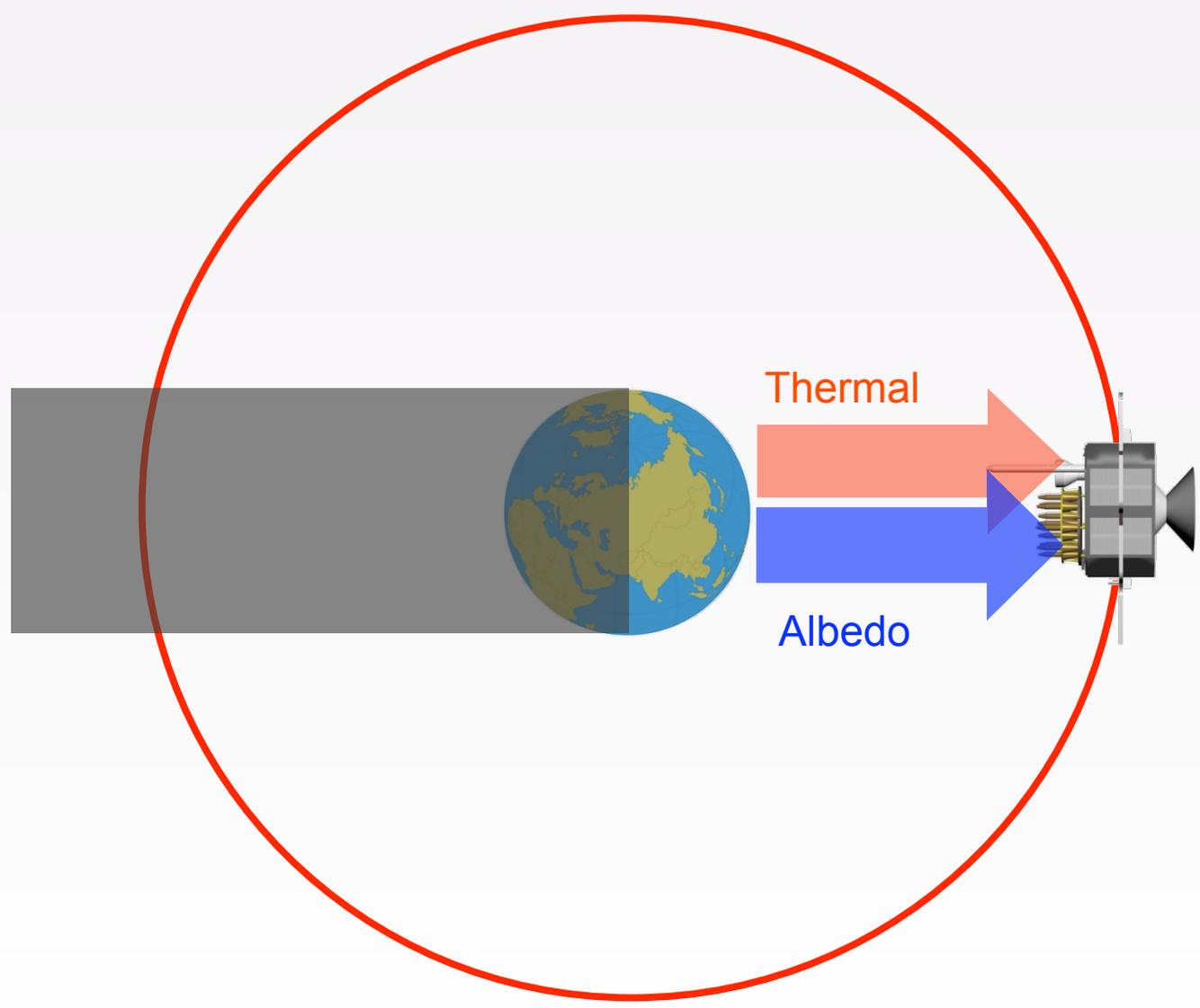


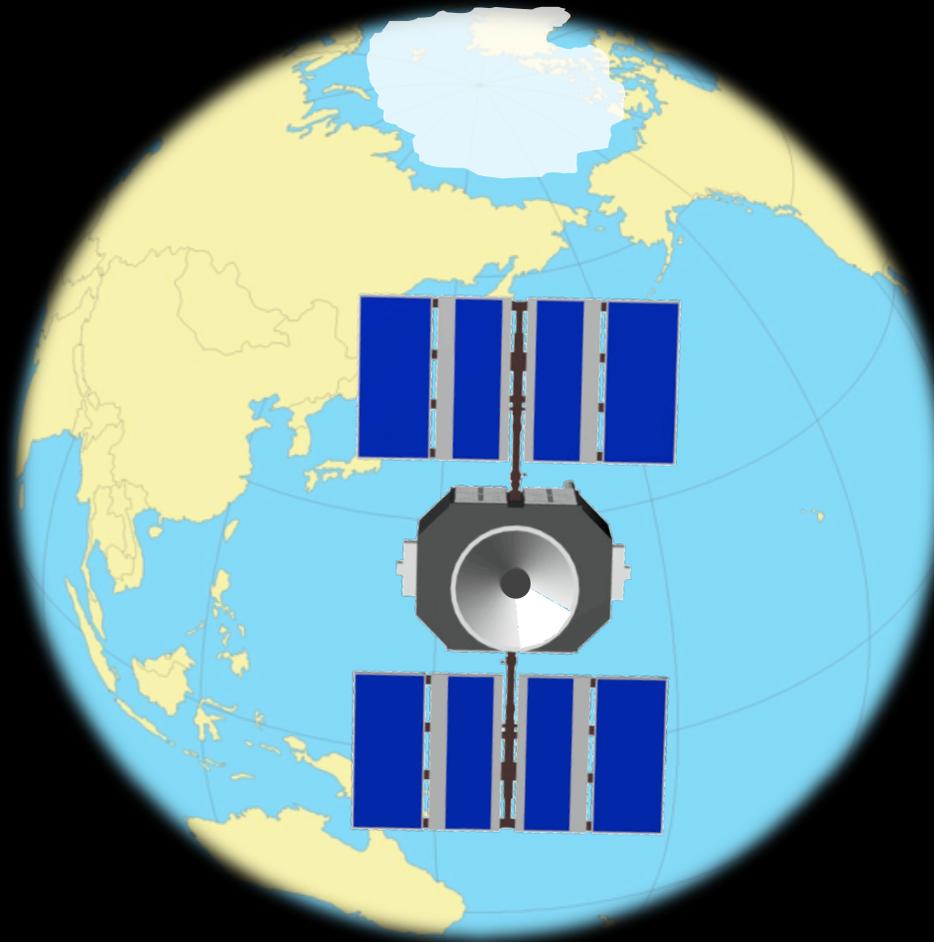




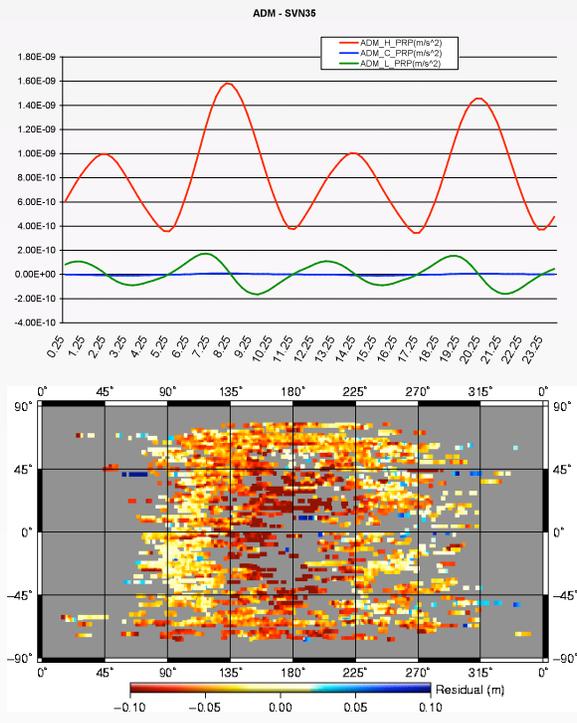




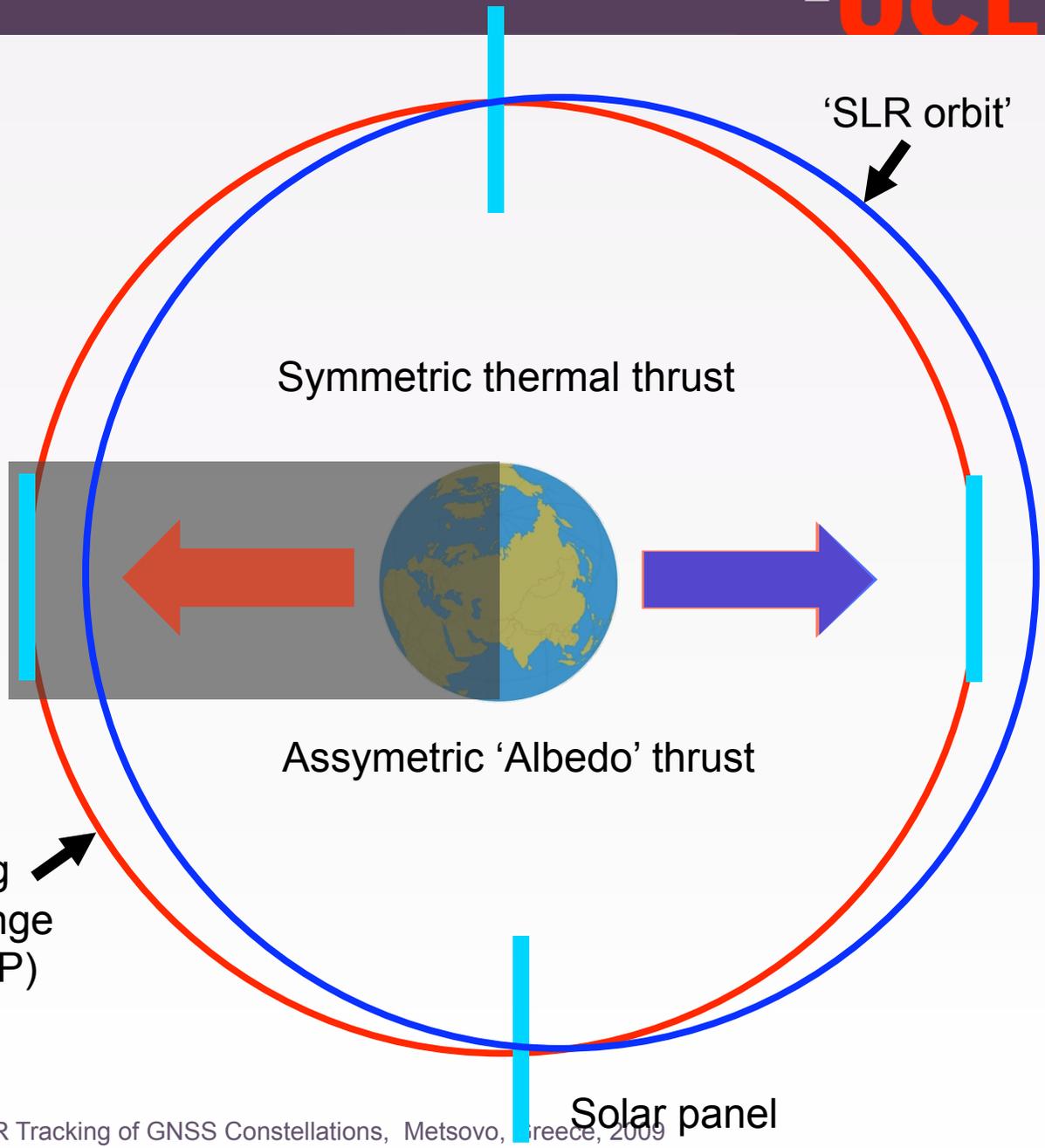




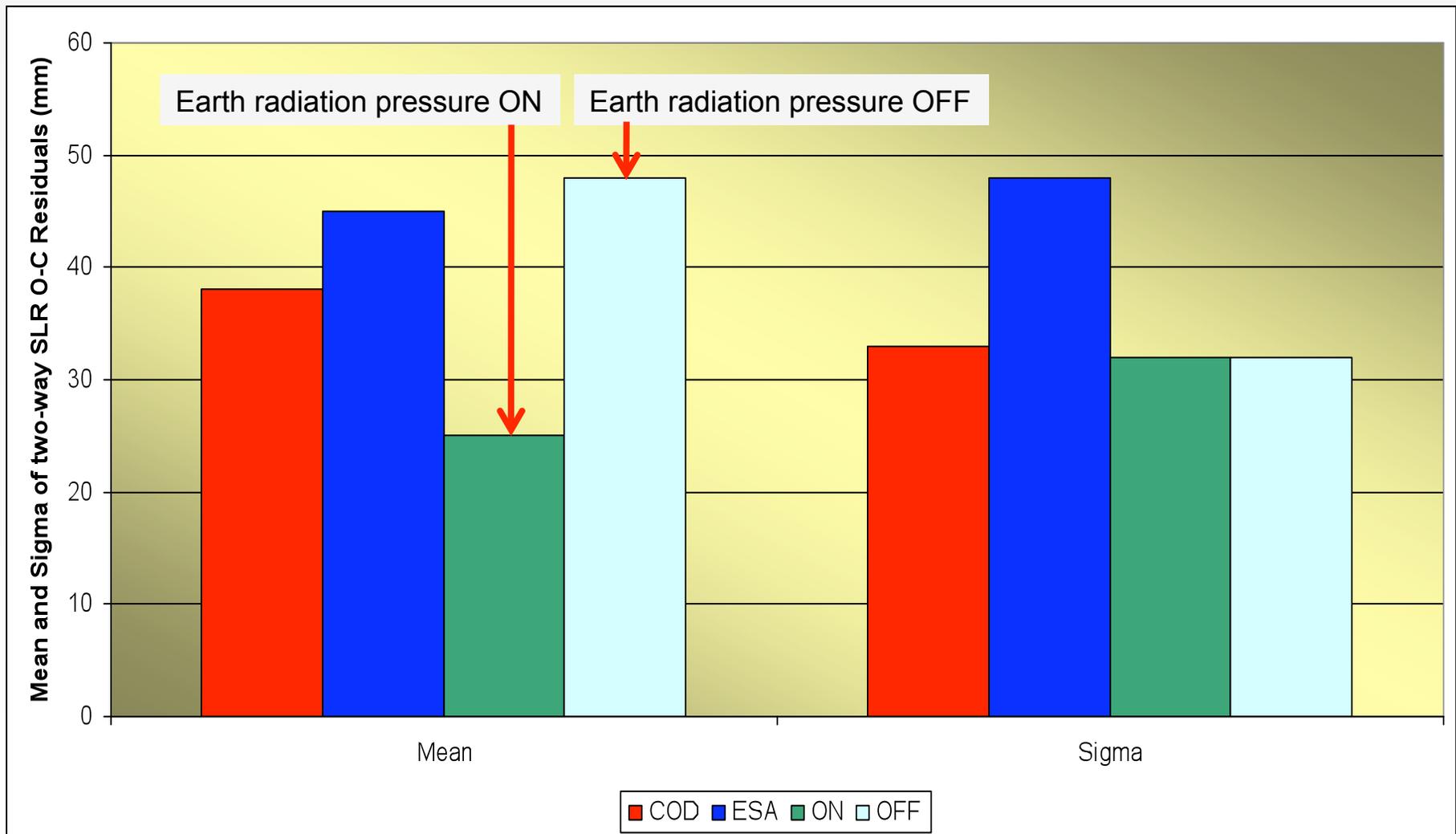
# Explanation



Orbit estimated using phase/pseudorange (without modelling PRP)



# SLR Validation of ESOC Reprocessed Orbits: Two way laser ranging residuals to SV35 and SV36



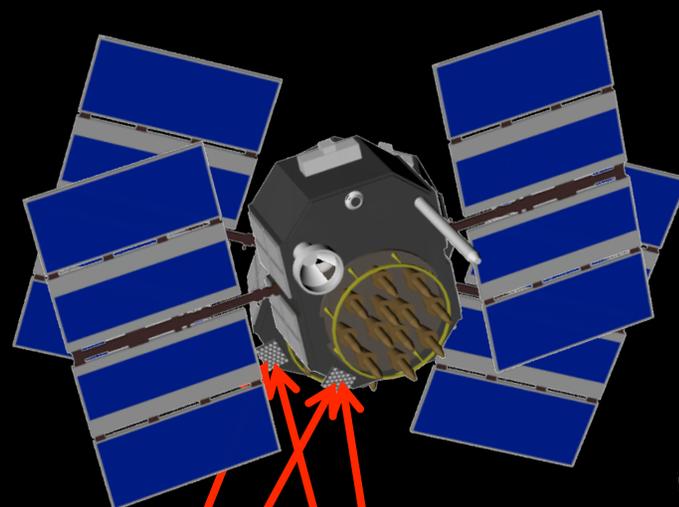
## Which PRP modelling method to adopt?

- Knocke-Ries model (basic, but proven, existing Fortran code)
- CERES/ERBE model, Lambert assumption
- CERES/ERBE Angular distribution model (ADM)
- ECMWF models (CNES implementation)
- CODE empirical model

## Multi-centre experiment, aims

- Participants: University of Berne; CNES; ESOC; JPL and UCL
- Test varying approaches to Earth radiation pressure modelling
- Assess impact on the GPS-SLR bias
- Assess impact of bias (and its elimination) on the global polyhedron, orbits, clocks, day boundary effect
- Assess impact on ITRF computation

# A brief comment on attitude: observing yaw state through SLR analysis



Can discriminate  
Yaw state through  
Laser analysis

## 1 or 2 cm bias on orbit? Why should we care?

- Altitude determination of satellite altimetry sensors
- Orbit prediction

# Gravity field mis-modelling in orbit prediction

Monopole acceleration:

$$a = -\frac{GM}{r^2}$$



$r$



Estimated position  
True position of satellite

Acceleration error:

$$\delta a = \frac{2GM\delta r}{r^3}$$

⇒ Acceleration error of:

⇒  $\sim 1.0 \times 10^{-9} \text{ ms}^{-2}$

⇒ Small number, big effect in time

⇒ Along track error of  $\sim 1.0\text{m}$  (12 hrs)

## Conclusions

- GPS-SLR bias primarily affects satellites either in, or near to, eclipse season (circa half the constellation at any one time)
- 'bias' reaches 4-5 cm around an arc on the dark side of the Earth (mean 'bias' =  $\sim 2$  cm)
- Modelling Earth Radiation Pressure effects significantly reduces the GPS-SLR bias
- Modelling antenna thrust reduces bias further
- Experiment underway to test impact on frame, clocks, orbits
- Great success story for the value of SLR data in system analysis